

$$130 \times \frac{\pi}{180}$$

$$A = \frac{1}{2} r^2 \theta$$

$$A = \frac{1}{2} (81)^2 \left( \frac{130\pi}{180} \right)$$

$$A = 7443.2 \text{ (W)}$$

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$$A = \frac{1}{2} (32)^2 \left( \frac{130\pi}{180} \right)$$

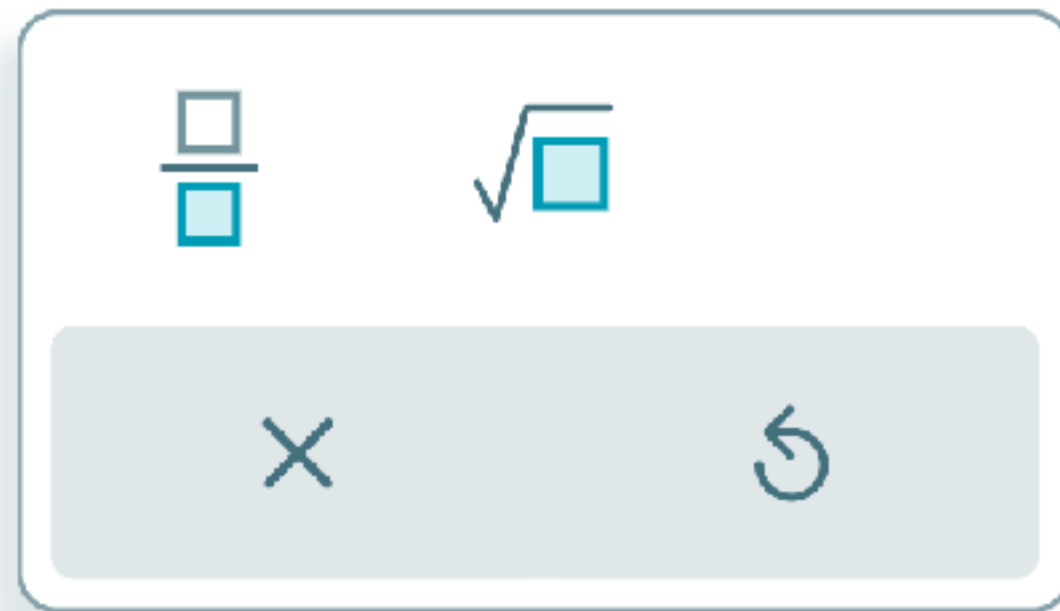
$$A = 1161.7 \text{ (M)}$$

If  $\theta = 135^\circ$ , find the exact value of each expression below.

(a)  $\cos(-\theta) =$

(b)  $\cos^2 \theta =$

(c)  $\cos 2\theta =$



$\theta = 135$   
 $\text{ref} = 45^\circ$   
 $\cos 45^\circ = \frac{\sqrt{2}}{2}$

$\cos^2 \theta$   
 $(\cos \theta)^2$   
 $\cos 135 = \left(-\frac{\sqrt{2}}{2}\right)^2 = \frac{2}{4} = \frac{1}{2}$


c)  $\cos(270)$

$$\tan 960^\circ = \boxed{\sqrt{3}}$$

$$\csc\left(-\frac{5\pi}{4}\right) = \boxed{\phantom{0}}$$

$$960 - 360 - 600 - 360$$

$$\tan(240)$$


$$\frac{\sin(60)}{\cos(60)}$$

$$\frac{\sqrt{3}/2}{1/2} = \sqrt{3}$$

$$\tan 960^\circ = \boxed{\sqrt{3}}$$

$$\csc\left(-\frac{5\pi}{4}\right) = \boxed{\phantom{0}}$$

$$\frac{2\sqrt{2}}{\sqrt{2}\sqrt{2}} = \frac{\cancel{2}\sqrt{2}}{\cancel{2}}$$

$$\csc\left(-\frac{5\pi}{4}\right)$$

$$-\frac{5\pi}{4} + 2\pi = \frac{3\pi}{4}$$

$$\csc \rightarrow \sin$$

$$\frac{1}{\sin(3\pi/4)} = \frac{1}{\sqrt{2}/2}$$

$$\frac{2}{\sqrt{2}} = \frac{2\sqrt{2}}{2} = \sqrt{2}$$

Find the period, amplitude, and phase shift of the function.

$$y = 4 \sin \left( \pi x + \frac{\pi}{4} \right) + 1$$

↑

a

$b x - c$

$$\left( \pi x + \frac{\pi}{4} \right)$$

Give the exact values, not decimal approximations.

Period:

2

Amplitude:

4

Phase shift:

$-\frac{1}{4}$

$\pi$

$$\pi \left( x + \frac{1}{4} \right)$$

↑

b

↑

Phase shift +

$$\text{Period} = \frac{2\pi}{b} = 2$$

Find the amplitude, phase shift, and period of the function.

$$y = -2 \sin\left(3x + \frac{\pi}{2}\right) - 1$$

← vertical shift

Give the exact values, not decimal approximations.

Amplitude:

Phase shift:

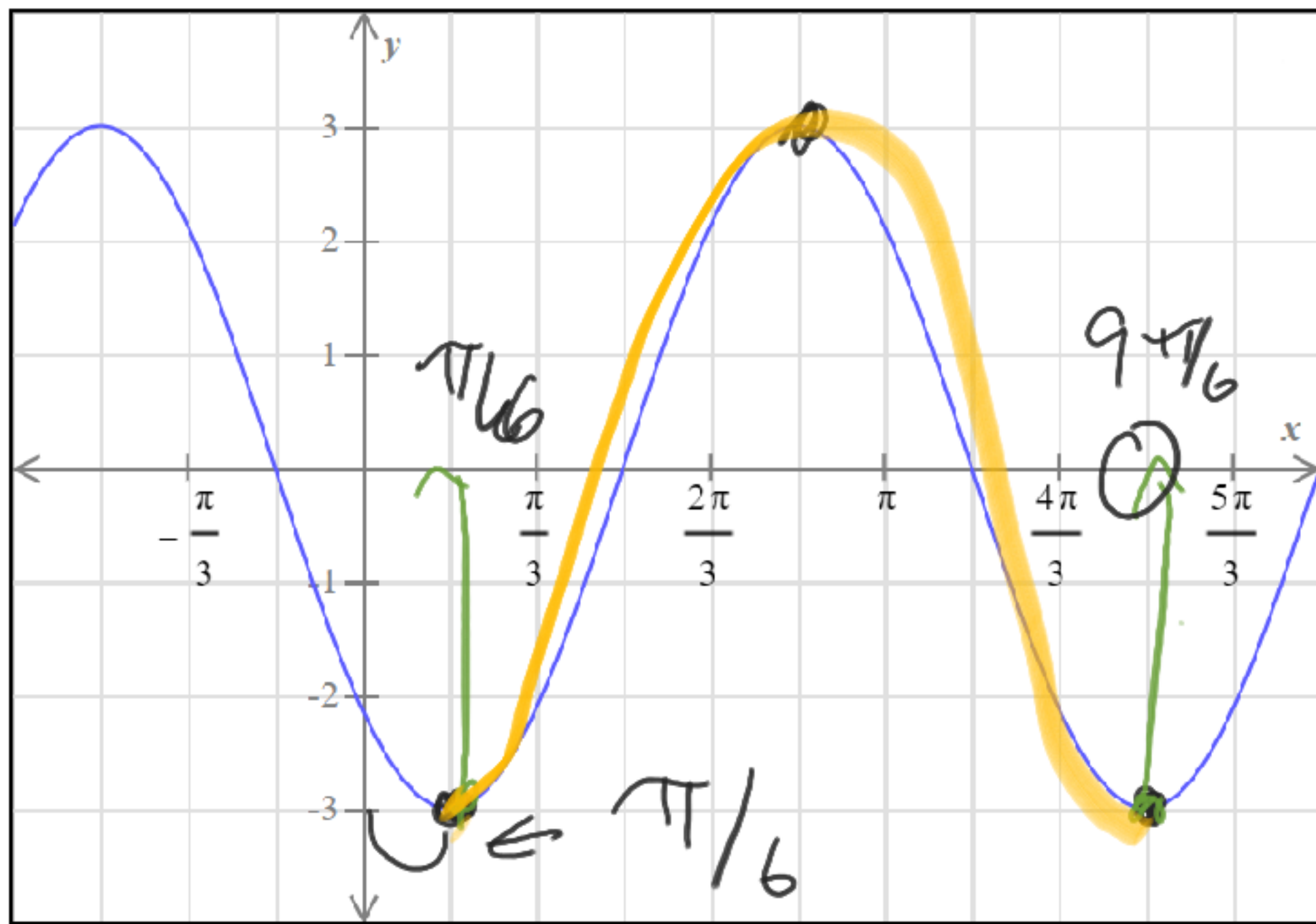
Period:

Calculator interface showing a fraction icon,  $\pi$ , a multiplication sign  $\times$ , and a left arrow  $\leftarrow$ .

$$3x + \frac{\pi}{2}$$
$$3\left(x + \frac{\pi}{6}\right)$$

↖ opposite ↗

period =  $\frac{2\pi}{3}$   $\frac{2}{3} \pi$



$$a \cos(b(x-c)) + d$$

$$-3 \cos\left(\frac{3}{2}(x-c)\right)$$

$$-3 \cos\left(\frac{3}{2}\left(x - \frac{\pi}{6}\right)\right)$$

$$\frac{9\pi}{6} - \frac{\pi}{6}$$

$$\text{period} = \frac{2\pi}{b} = \frac{2\pi}{\frac{3}{2}} = \frac{4\pi}{3}$$

$$8\pi b = 12\pi$$

The population sizes of many animal species rise and fall over time. Suppose that the population function.

$$p(t) = 3050 + 1250 \cos 1.5t$$

*Handwritten annotations:*  $d$  above 3050,  $a$  above 1250,  $3050 \uparrow$  to the right of the equation. A graph to the right shows a cosine wave oscillating around a horizontal line.

In this equation,  $p(t)$  represents the total population size, and  $t$  is the time in years.

Find the following. If necessary, round to the nearest hundredth.

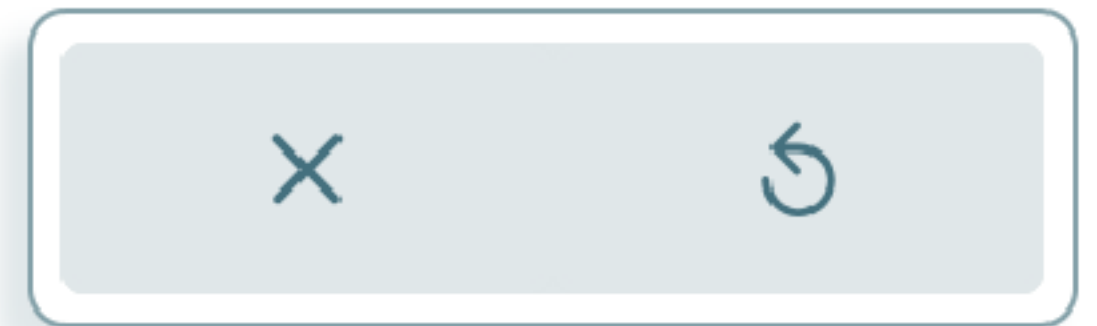
Minimum population size:

Time for one full cycle of  $p$  :  years

Number of cycles of  $p$  per year:

$$\text{max } 3050 + 1250 = 4300$$

$$\text{min } 3050 - 1250 = 1800$$





The population sizes of many animal species rise and fall over time. Suppose that the population function.

$$p(t) = 3050 + 1250 \cos 1.5t$$

$$\text{Period} = \frac{2\pi}{b} = \frac{2\pi}{1.5}$$

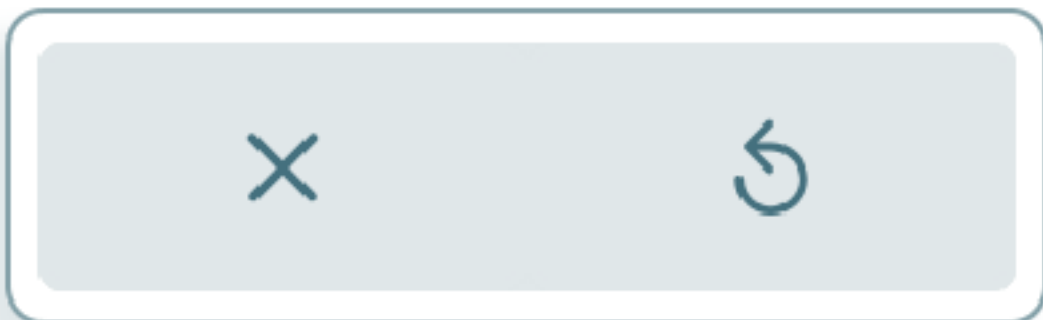
In this equation,  $p(t)$  represents the total population size, and  $t$  is the time in years.

Find the following. If necessary, round to the nearest hundredth.

Minimum population size:

Time for one full cycle of  $p$  :  years 4.19

Number of cycles of  $p$  per year:  0.24

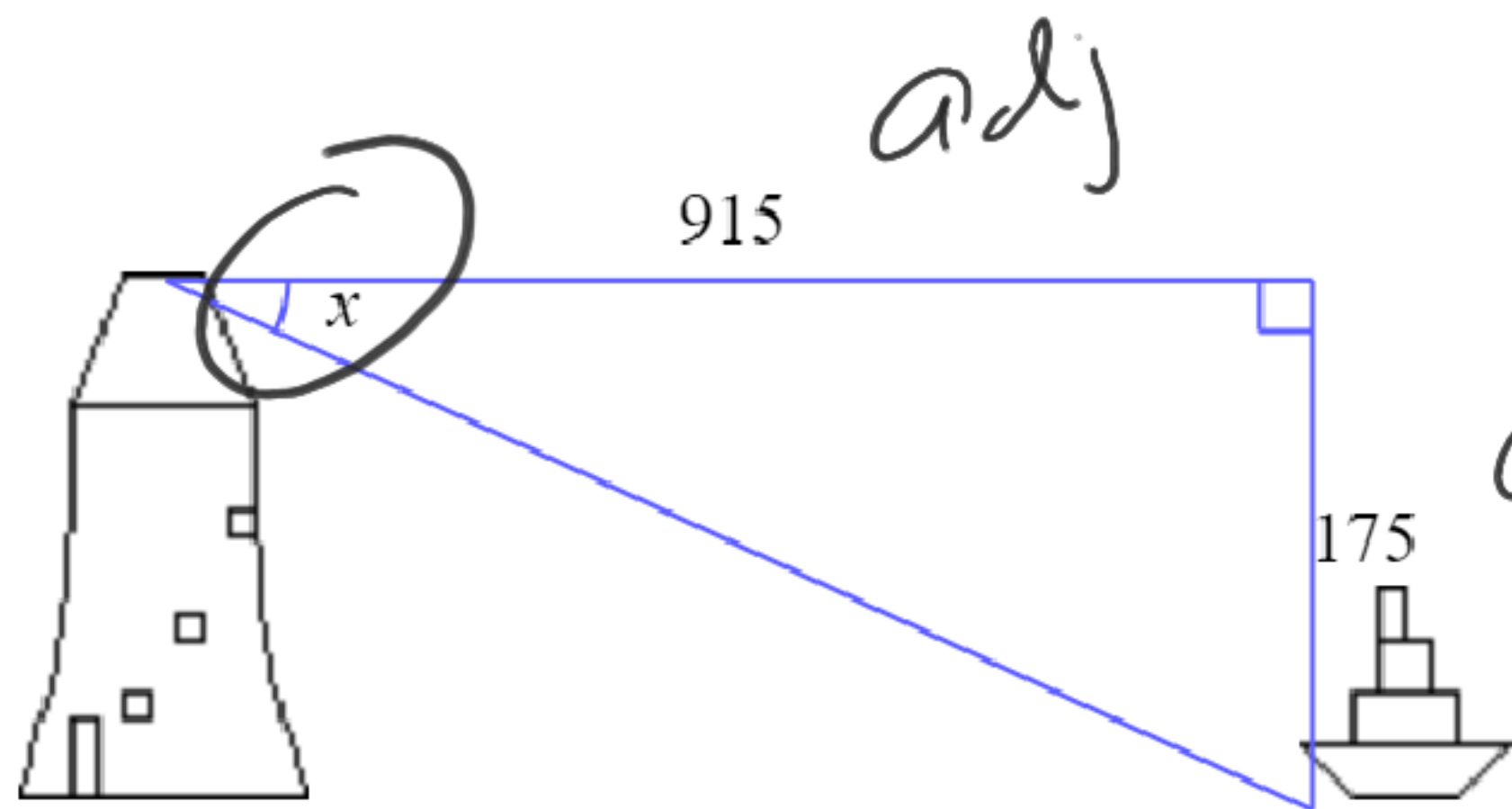


$$1 / 4.19 = 0.24$$

Graph the trigonometric function.

$$y = 2 \cos \left( x - \frac{2\pi}{3} \right)$$

$x + \frac{2\pi}{3}$	$x$	$y$	$2y$
$2\pi/3$	$0$	$1$	$2$
$7\pi/6$	$\pi/2$	$0$	$0$
$5\pi/3$	$\pi$	$-1$	$-2$
$13\pi/6$	$3\pi/2$	$0$	$0$
$8\pi/3$	$2\pi$	$1$	$2$



$$X = 10,8^\circ$$

~~$$\tan^{-1}(\tan X) = \tan^{-1}\left(\frac{175}{915}\right)$$~~

X

Suppose a weight on a pendulum swings back and forth in simple harmonic motion.

The following equation describes the weight's horizontal displacement  $d$  (in centimeter)  
Note that rightward is the positive direction.

$$d = 35 \sin\left(\frac{5\pi}{6}t\right)$$

$\frac{6}{5}\pi X$	X	Y	35y
0	0	0	0
$\frac{3}{5}$	$\frac{\pi}{2}$	1	35
$\frac{6}{5}$	$\pi$	0	0
$\frac{9}{5}$	$\frac{3\pi}{2}$	-1	-35
$\frac{12}{5}$	$2\pi$	0	0

